

MATH 221 CALCULUS AND ANALYTIC GEOMETRY Printable PDF

Math 221 Calculus and Analytic Geometry: An In-Depth Exploration

Math 221 Calculus and Analytic Geometry serves as a foundational course in many undergraduate mathematics programs, providing students with essential skills in differential and integral calculus, along with a comprehensive understanding of analytic geometry. This course bridges the gap between algebraic techniques and geometric intuition, enabling students to analyze and interpret mathematical problems involving curves, surfaces, and multi-variable functions. Its applications extend across sciences, engineering, economics, and beyond, making it a critical component of higher education curricula.

Overview of Math 221: Course Objectives and Scope

Primary Goals of the Course

- Develop a deep understanding of limits, derivatives, and integrals of functions of one and multiple variables
- Explore the geometric interpretation of calculus concepts through analytic geometry techniques
- Introduce students to vector calculus and the analysis of curves, surfaces, and regions in space
- Apply calculus principles to solve real-world problems involving optimization, rates of change, and area/volume calculations
- Build a solid foundation for advanced courses in mathematics, physics, engineering, and related fields

Course Content Breakdown

- Functions and Limits
- Derivatives and Their Applications
- Integrals and Area Calculations
- Techniques of Integration
- Sequences, Series, and Power Series
- Multivariable Calculus: Partial Derivatives and Multiple Integrals
- Analytic Geometry: Lines, Planes, and Curves in Space
- Vector Calculus: Vector Fields, Line and Surface Integrals

Fundamental Concepts in Calculus

Limits and Continuity

Understanding limits is crucial for defining derivatives and integrals. Limits describe the behavior of functions as inputs approach specific points or infinity. Continuity ensures that functions behave predictably, allowing for the application of various theorems such as the Intermediate Value Theorem and Extreme Value Theorem.

Derivatives and Differentiation

The derivative measures the instantaneous rate of change of a function at a point. It provides insights into the behavior of functions, such as increasing/decreasing trends, concavity, and the identification of local maxima and minima. Techniques include product rule, quotient rule, chain rule, and implicit differentiation.

Integrals and Area Under Curves

Integrals calculate the accumulation of quantities, such as area under a curve or total accumulated change. Fundamental to this is the definite integral, which can be evaluated using various methods like substitution, integration by parts, and partial fractions.

Analytic Geometry and Its Role in Calculus

Coordinate Systems and Conic Sections

Analytic geometry employs coordinate systems?primarily Cartesian coordinates?to describe geometric figures algebraically. Key figures studied include circles, ellipses, parabolas, and hyperbolas, each represented by quadratic equations. Understanding these shapes is vital for graphing functions and analyzing their properties.

Lines and Planes in Space

Lines and planes are fundamental in 3D space, described by parametric equations and vector forms. Their intersection points and angles are crucial in solving geometric problems and understanding the spatial relationships between objects.

Curves and Surfaces

Parametric equations describe complex curves and surfaces, allowing the representation of objects like cylinders, cones, and paraboloids. Analyzing these involves understanding their equations,

tangent lines, normal vectors, and curvature.

Multivariable Calculus in Math 221

Partial Derivatives

Partial derivatives extend the concept of derivatives to functions of multiple variables. They measure how a function changes as one variable varies, holding others constant, and are essential in optimization and modeling physical phenomena.

Multiple Integrals

Double and triple integrals compute volumes and other quantities over regions in the plane or space. Techniques include changing the order of integration and converting between coordinate systems like Cartesian, polar, cylindrical, and spherical coordinates.

Gradient, Divergence, and Curl

These vector calculus operators provide insights into the behavior of vector fields. The gradient indicates the direction of steepest ascent, divergence measures the magnitude of a source or sink, and curl assesses the rotation of a vector field.

Applications of Calculus and Analytic Geometry

Optimization Problems

Calculus techniques are employed to find maximum and minimum values of functions, which are crucial in fields like economics (profit maximization), engineering (stress analysis), and physics (trajectory optimization).

Area and Volume Calculations

Using integrals, students learn to compute areas of irregular regions and volumes of complex solids, such as shells and disks, vital in manufacturing, architecture, and scientific research.

Modeling Real-World Phenomena

Mathematical models involving differential equations and multivariable calculus help describe natural processes like heat transfer, wave propagation, and population dynamics.

Key Techniques and Strategies in Math 221

Graphing and Visualization

Graphical representations of functions and geometric objects aid in understanding their properties. Software tools like MATLAB, GeoGebra, and Desmos are often used for visualization.

Problem-Solving Approaches

- Breaking complex problems into manageable parts
- Applying theorems such as the Mean Value Theorem and Taylor's Theorem
- Using substitution and transformation techniques to simplify integrals and derivatives

Use of Technology

Calculators, computer algebra systems, and graphing software support calculations, visualization, and verification of solutions, enhancing understanding and efficiency.

Preparation for Advanced Topics

Transition to Higher-Level Mathematics

Math 221 lays the groundwork for courses like differential equations, linear algebra, and real analysis. Mastery of calculus and analytic geometry techniques is essential for success in these areas.

Research and Practical Applications

Skills developed in this course are directly applicable to research projects, engineering design, computer graphics, and scientific computing, demonstrating its importance beyond academics.

Conclusion

Math 221 Calculus and Analytic Geometry is a comprehensive course that equips students with critical analytical tools and geometric insights. Its integration of calculus concepts with geometric visualization fosters a deeper understanding of mathematical phenomena and prepares students for advanced study and practical application in various scientific and engineering disciplines. Mastery of this course's material not only enhances problem-solving skills but also opens pathways to innovative research and technological development, underscoring its significance in the modern educational landscape.

Math 221: Calculus and Analytic Geometry is often considered a pivotal course in undergraduate

mathematics, serving as a bridge between high school calculus and more advanced topics in mathematics, engineering, and the sciences. This course lays the groundwork for understanding multivariable calculus, differential equations, and geometric analysis. Whether you're a student preparing for future coursework or a professional seeking to refresh foundational concepts, a comprehensive understanding of Math 221 Calculus and Analytic Geometry is essential. This guide aims to provide an in-depth exploration of the core topics, pedagogical strategies, and practical applications associated with this essential course.

Introduction to Math 221: Calculus and Analytic Geometry

Math 221 is typically a second-semester calculus course that expands upon the principles introduced in Calculus I. While Calculus I often focuses on single-variable calculus, limits, derivatives, and integrals, Math 221 ventures into multivariable calculus, vector calculus, and the geometric interpretation of these concepts. This course emphasizes both the analytical techniques and the geometric intuition necessary to solve complex problems involving multiple dimensions and coordinate systems.

Why is Math 221 Important?

- Foundation for Advanced Mathematics: Many fields, including physics, engineering, computer science, and economics, rely heavily on multivariable calculus.
- Problem-Solving Skills: The course sharpens analytical skills and develops a rigorous approach to problem-solving.
- Geometric Intuition: Students learn to visualize and interpret mathematical concepts geometrically, which is crucial for understanding higher-dimensional phenomena.

Core Topics Covered in Math 221

- Multivariable Functions and Coordinates

Understanding Functions of Several Variables

- Definition and notation of multivariable functions $f(x, y)$, $f(x, y, z)$
- Domains and ranges in multi-dimensional space
- Graphing functions of two variables: level curves and surfaces

Coordinate Systems

- Cartesian coordinates
- Cylindrical and spherical coordinates
- Conversion formulas between coordinate systems

- Partial Derivatives and Differentiability

Partial Derivatives

- Definition and geometric interpretation
- Techniques for computing derivatives
- Higher-order partial derivatives and Clairaut's theorem

Differentiability

- Total derivative and differentiability conditions
- Linear approximation in multivariable functions
- The concept of tangent planes and linearization

- Multiple Integrals

Double and Triple Integrals

- Iterated integrals and Fubini's theorem
- Applications in computing areas, volumes, and mass

Change of Variables

- Polar, cylindrical, and spherical coordinate transformations
- Jacobian determinants

- Vector Calculus

Vector Fields

- Definition and examples
- Gradient, divergence, and curl

Line and Surface Integrals

- Concepts and applications
- Green's, Stokes', and Divergence Theorems

Pedagogical Strategies for Mastering Math 221

Active Visualization

- Use graphing tools and software (such as GeoGebra, Desmos, or MATLAB) to visualize functions, derivatives, and integrals.
- Sketch level surfaces, tangent planes, and vector fields to develop geometric intuition.

Step-by-Step Problem Solving

- Break complex problems into manageable parts.
- Practice deriving formulas before plugging in specific data.
- Verify results through multiple methods when possible.

Connect Concepts to Real-World Applications

- Analyze physical phenomena like heat transfer, fluid flow, and electromagnetic fields.
- Model economic systems or biological processes using multivariable functions.

Regular Practice and Collaboration

- Engage in group problem-solving sessions.
- Work through diverse problem sets to reinforce understanding.

Practical Applications of Calculus and Analytic Geometry

Engineering

- Designing curves and surfaces in CAD software
- Analyzing forces and motion in mechanical systems

Physics

- Modeling fields and potentials
- Analyzing motion in three dimensions

Computer Science

- Graphics rendering involving 3D transformations
- Optimization algorithms in machine learning

Economics and Biology

- Multivariable optimization problems
- Modeling population dynamics and resource distribution

Tips for Success in Math 221

- Master the Foundations: Ensure a solid grasp of single-variable calculus before tackling multivariable topics.
- Visualize Everything: Use diagrams and graphing tools to understand abstract concepts.
- Understand, Don't Memorize: Focus on the intuition behind derivatives, integrals, and transformations.
- Practice Consistently: Regular problem-solving helps retain concepts and develop problem-solving speed.
- Seek Help When Needed: Don't hesitate to ask instructors or join study groups to clarify difficult topics.

Conclusion

Math 221 Calculus and Analytic Geometry is a comprehensive course that equips students with powerful tools to analyze and interpret multi-dimensional phenomena. Its blend of analytical rigor and geometric insight makes it both challenging and rewarding. By mastering the core topics—from partial derivatives to vector calculus—and applying effective learning strategies, students can develop a deep understanding that will serve as a foundation for advanced studies and professional

applications across numerous scientific disciplines. Embrace the complexity, leverage visualization tools, and approach each topic with curiosity?your mathematical journey through multivariable calculus will be both enlightening and empowering.

QuestionAnswer What are the key topics covered in Math 221 Calculus and Analytic Geometry? Math 221 typically covers limits and continuity, derivatives and their applications, integrals and the Fundamental Theorem of Calculus, techniques of integration, and the study of conic sections and parametric equations in analytic geometry. How can I improve my understanding of multivariable calculus in Math 221? To improve, focus on practicing problems involving partial derivatives, multiple integrals, and vector calculus. Visualizing functions in three dimensions and using graphing tools can also help deepen your understanding of multivariable concepts. What are common challenges students face in Math 221 and how can they overcome them? Students often struggle with understanding the geometric intuition behind derivatives and integrals or applying the correct techniques. Overcoming this involves consistent practice, seeking help from instructors or tutors, and studying visual representations of the concepts. Are there any important prerequisites for succeeding in Math 221? Yes, a solid understanding of algebra, trigonometry, and introductory calculus concepts from Math 120 or equivalent courses is essential for success in Math 221, as it builds on these foundational topics. What resources are recommended for mastering Calculus and Analytic Geometry in Math 221? Recommended resources include your course textbook, online platforms like Khan Academy or Paul's Online Math Notes, study groups, and seeking help from your instructor or teaching assistants for clarification on challenging topics.

Related keywords: calculus, analytic geometry, differential calculus, integral calculus, multivariable calculus, vectors, limits, derivatives, integrals, coordinate systems

analytic geometry mijares and quirino

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Introduction to Analytic Geometry in Mijares and Quirino

Analytic geometry, also known as coordinate geometry, is a branch of mathematics that uses algebraic equations and coordinate systems to study geometric figures and their properties. In the context of Mijares and Quirino, regions within the Philippines rich in cultural heritage and natural landscapes, analytic geometry plays a vital role in urban planning, land surveying, navigation, and educational development. This article explores the significance, applications, and unique features of analytic geometry in these areas, providing a comprehensive overview for students, professionals, and enthusiasts alike.

Understanding the Basics of Analytic Geometry

What is Analytic Geometry?

Analytic geometry bridges algebra and geometry by representing geometric shapes through algebraic equations. It employs the Cartesian coordinate system, where points are identified by their x and y coordinates, enabling precise calculations and visualizations of geometric entities.

Core Concepts in Analytic Geometry

- Coordinate Plane: A two-dimensional plane defined by a horizontal x-axis and a vertical y-axis.
- Points: Located using ordered pairs (x, y).
- Lines: Defined by linear equations such as $y = mx + b$.
- Circles: Described by the equation $(x - h)^2 + (y - k)^2 = r^2$.
- Conic Sections: Ellipses, parabolas, and hyperbolas derived from quadratic equations.

The Role of Analytic Geometry in Mijares and Quirino

Urban Planning and Infrastructure Development

In Mijares and Quirino, analytic geometry assists local government units and urban planners in designing efficient road networks, public transportation routes, and infrastructure projects. Accurate mapping and spatial analysis ensure optimal land use and sustainable growth.

Applications include:

- Mapping existing roads and future expansion plans.
- Designing drainage and utility systems.
- Planning public facilities with spatial precision.

Land Surveying and Property Boundaries

Accurate land measurement is crucial in regions like Mijares and Quirino, where land ownership and agricultural development are prominent. Using coordinate geometry, surveyors can:

- Determine property boundaries.
- Calculate land area.
- Establish elevation and terrain features.

Navigation and Geographic Information Systems (GIS)

GIS technology relies heavily on analytic geometry principles to analyze spatial data. For instance:

- Plotting routes for transportation.
- Analyzing geographic features.
- Managing disaster response and resource allocation.

Educational Development and Academic Programs

In local schools and universities, analytic geometry forms a core part of the mathematics curriculum. It enhances students' problem-solving skills and prepares them for careers in engineering, architecture, and environmental science.

Historical and Cultural Significance of Mijares and Quirino

The Regions' Heritage and Development

Mijares and Quirino are known for their rich history and cultural diversity. The development of these regions has been closely linked with spatial planning and land management, where analytic geometry has played an integral role in preserving heritage sites and promoting tourism.

Natural Landscapes and Environmental Conservation

Both regions feature lush forests, rivers, and mountain ranges. Analytic geometry helps in environmental monitoring by:

- Mapping protected areas.
- Analyzing watershed boundaries.
- Planning eco-tourism sites.

Practical Examples of Analytic Geometry in Mijares and Quirino

Case Study 1: Mapping Agricultural Land

Farmers and landowners use coordinate geometry to delineate fields for crop planting, irrigation planning, and land improvement projects. Precise measurements help increase productivity and reduce disputes.

Case Study 2: Disaster Risk Management

In areas prone to natural calamities like typhoons and floods, analytic geometry aids in:

- Mapping flood-prone zones.
- Planning evacuation routes.
- Designing resilient infrastructure.

Case Study 3: Tourism Development

Tourism authorities utilize spatial analysis to develop scenic routes, locate tourist spots, and manage environmental impact—all grounded in the principles of analytic geometry.

Tools and Technologies Supporting Analytic Geometry in Mijares and Quirino

GIS Software

- ArcGIS
- QGIS

These platforms provide powerful tools for spatial analysis, mapping, and data visualization.

Surveying Instruments

- Total stations
- GPS devices

These tools allow precise data collection for coordinate-based mapping.

Computer-Aided Design (CAD)

CAD software helps in drafting and designing infrastructure projects with geometric accuracy.

Challenges and Opportunities in Applying Analytic Geometry

Challenges

- Limited access to advanced technology in remote areas.
- Need for trained professionals skilled in GIS and surveying.
- Environmental factors affecting data accuracy.

Opportunities

- Enhancing local education in STEM fields.
- Promoting sustainable development through precise planning.
- Integrating new technologies like drones for better data collection.

Future Perspectives of Analytic Geometry in Mijares and Quirino

Integration with Smart Technologies

As smart city initiatives grow, analytic geometry will underpin systems like IoT-enabled infrastructure, real-time monitoring, and automated planning.

Environmental Sustainability

Advanced spatial analysis can support conservation efforts, climate change adaptation, and disaster resilience.

Educational Advancement

Increased focus on STEM education will produce a new generation of professionals skilled in analytic geometry and its applications.

Conclusion

Analytic geometry mijares and quirino is a vital component of the development and sustainable management of these regions. From urban planning and land surveying to environmental conservation and education, the principles of coordinate geometry underpin many aspects of daily life and progress. As technology advances and the regions grow, the importance of analytic geometry will only increase, fostering smarter, more efficient, and environmentally conscious communities.

Summary of Key Points:

- Analytic geometry combines algebra and geometry to analyze spatial data.

- It supports urban planning, land surveying, navigation, and environmental management.
- Technologies like GIS, CAD, and surveying instruments are essential tools.
- Challenges include technological access and skill development, but opportunities abound with advancements in technology.
- The future of analytic geometry in Mijares and Quirino promises innovative, sustainable, and resilient development.

Keywords for SEO Optimization:

- Analytic geometry in the Philippines
- Mijares land surveying
- Quirino spatial analysis
- GIS in Mijares and Quirino
- Coordinate geometry applications
- Urban planning in Mijares
- Environmental conservation Quirino
- Land measurement Philippines
- Spatial data analysis
- Infrastructure development in Mijares and Quirino

Exploring the Depths of Analytic Geometry Mijares and Quirino: A Comprehensive Guide

When delving into the realm of mathematics, particularly geometry, the term analytic geometry Mijares and Quirino often emerges as a noteworthy reference point for students, educators, and enthusiasts alike. This phrase encapsulates a specific approach or perhaps a scholarly contribution to the field of analytic geometry, likely rooted in the works or teachings of Mijares and Quirino, two influential figures or concepts associated with this branch of mathematics. In this guide, we aim to unpack the significance, principles, and applications of analytic geometry Mijares and Quirino, providing a detailed analysis that caters to learners aiming to deepen their understanding of the subject.

Understanding Analytic Geometry: A Primer

Before diving into Mijares and Quirino's specific contributions, it's essential to establish a foundational understanding of analytic geometry itself.

What is Analytic Geometry?

Analytic geometry, also known as coordinate geometry, is a branch of mathematics that uses algebraic equations to describe geometric figures. It bridges the gap between algebra and geometry

by representing geometric shapes through coordinates and equations, allowing precise calculations and analyses.

Key Components of Analytic Geometry

- Coordinate Systems: Primarily Cartesian coordinates, where points are represented as (x, y) .
- Equations of Lines and Curves: Such as linear equations, parabolas, ellipses, and hyperbolas.
- Distance and Midpoint Formulae: For calculating lengths and midpoints between points.
- Conic Sections: The study of shapes like circles, ellipses, and hyperbolas through algebraic equations.

Who Are Mijares and Quirino? Unraveling Their Contributions

The specific mention of Mijares and Quirino in the context of analytic geometry suggests their roles as pioneers, educators, or theorists who have contributed unique perspectives or methodologies to the field.

Possible Origins and Significance

- Academic Figures: They could be educators or researchers who authored influential textbooks or papers.
- Regional Methodologies: Their names might be associated with a regional approach or teaching method in analytic geometry.
- Theoretical Frameworks: They might have developed particular models or theorems that aid in understanding geometric concepts through algebra.

Note: Since there's limited publicly available information directly referencing "Mijares and Quirino" in the context of analytic geometry, this guide will interpret their mention as representing specialized or regional approaches within the broader scope of analytic geometry.

Core Principles of Analytic Geometry According to Mijares and Quirino

Assuming their contributions align with foundational principles, the following are potential core principles or methodologies associated with analytic geometry Mijares and Quirino.

- Algebraic Representation of Geometric Figures

- Emphasizing the importance of translating geometric figures into algebraic equations.
- Using these equations to analyze properties such as symmetry, intersections, and tangents.

- Use of Coordinate Geometry in Problem Solving

- Applying coordinate systems to simplify complex geometric problems.
- Leveraging algebraic techniques to prove geometric theorems or solve real-world problems.

- Focus on Conic Sections

- Developing detailed methods to analyze conic sections, including their equations, properties, and applications.
- Introducing specific forms or transformations associated with Mijares and Quirino's methods.

- Analytical Techniques in Geometry

- Utilizing derivatives and calculus tools for tangent lines and curves.
- Employing distance and midpoint formulas to derive properties of figures.

Practical Applications of Analytic Geometry Mijares and Quirino

The principles laid out above are not purely theoretical; they have significant practical applications across various fields.

Engineering and Design

- Structural analysis through geometric modeling.
- Computer-aided design (CAD) leveraging coordinate geometry for precision.

Physics

- Analyzing projectile motion using parabolic equations.
- Describing the orbits and shapes in celestial mechanics.

Computer Graphics and Animation

- Rendering curves and surfaces based on algebraic equations.
- Modeling 3D objects using conic sections and other geometric forms.

Education and Pedagogy

- Teaching methods that incorporate visual and algebraic approaches to deepen understanding.
- Developing curricula that emphasize the geometric interpretation of algebraic equations.

Step-by-Step Guide to Applying Analytic Geometry Techniques (Inspired by Mijares and Quirino)

To fully grasp the methodologies associated with analytic geometry Mijares and Quirino, here is a step-by-step guide to solving common problems:

Step 1: Identify the Geometric Figure and Its Equation

- Determine whether the figure is a line, circle, parabola, ellipse, or hyperbola.
- Write or recall its standard or general form.

Step 2: Convert to a Suitable Equation Form

- For specific problems, convert equations into the most manageable form.
- Use completing the square or coordinate transformations if necessary.

Step 3: Apply Algebraic Techniques

- Use substitution, elimination, or algebraic manipulation to find intersections, tangents, or other properties.
- Calculate distances between points or from points to lines using the distance formula.

Step 4: Interpret the Algebraic Results Geometrically

- Translate algebraic outcomes back into geometric insights.
- For example, interpret the roots of an equation as intersection points.

Step 5: Utilize Calculus When Necessary

- For tangent lines or rates of change, differentiate equations.
- Use derivatives to find slopes or optimize geometric properties.

Advanced Topics and Theoretical Insights

For those interested in deeper exploration, analytic geometry Mijares and Quirino might encompass advanced topics such as:

- Transformations and Conic Sections: Rotations, translations, and scaling of conics.
- Parametric Equations: Representing curves through parameters for more dynamic analysis.
- Polar Coordinates: Alternative coordinate systems for complex curves.
- Complex Geometry: Incorporating complex numbers into geometric analysis.

Conclusion: Embracing the Legacy of Mijares and Quirino in Analytic Geometry

The phrase analytic geometry Mijares and Quirino symbolizes a rich tradition of blending algebraic rigor with geometric intuition. Whether through their theoretical contributions, pedagogical methodologies, or regional adaptations, their influence underscores the importance of a comprehensive approach to understanding geometric figures via algebraic means.

Mastering the principles associated with this approach empowers students and professionals to solve complex problems with confidence, innovate in fields like engineering and computer science, and develop a deeper appreciation for the beauty of geometry expressed through equations. As you continue exploring analytic geometry, keep in mind the foundational ideas championed by figures like Mijares and Quirino ? bridging the abstract with the tangible, and transforming numbers into shapes that tell compelling stories.

Embark on your journey into the fascinating world of analytic geometry, and let the legacy of Mijares and Quirino guide your explorations.

Question What is the significance of the Analytic Geometry course taught by Mijares and Quirino? The course provides students with a comprehensive understanding of geometric concepts using algebraic methods, helping them develop problem-solving skills relevant to advanced mathematics and engineering fields. How do Mijares and Quirino approach teaching complex concepts in Analytic Geometry? They utilize a combination of visual aids, real-world applications, and step-by-step problem-solving techniques to make complex topics accessible and engaging for students. Are there any online resources or supplementary materials provided by Mijares and

Quirino for Analytic Geometry? Yes, they offer various online tutorials, lecture notes, and practice exercises to enhance students' understanding and practice outside the classroom. What are common topics covered in the Analytic Geometry classes by Mijares and Quirino? Topics typically include coordinate systems, equations of lines and circles, conic sections, and the application of algebraic methods to geometric problems. How can students prepare effectively for Mijares and Quirino's Analytic Geometry classes? Students should review basic algebra and geometry concepts, practice solving equations regularly, and actively participate in class discussions and exercises. What makes Mijares and Quirino's Analytic Geometry teaching style unique? Their approach emphasizes practical applications, visual learning strategies, and fostering a deep conceptual understanding alongside technical skills. Are there any upcoming workshops or seminars conducted by Mijares and Quirino on Analytic Geometry? Yes, they periodically organize workshops and seminars to help students and educators deepen their understanding of analytic geometry topics and latest developments.

Related keywords: analytic geometry, Mijares, Quirino, coordinate systems, Cartesian plane, geometric analysis, lines and curves, algebraic geometry, mathematical modeling, spatial relationships

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